

# ACCURATE LINEAR THERMAL EXPANSION COEFFICIENT DETERMINATION BY INTERFEROMETRY

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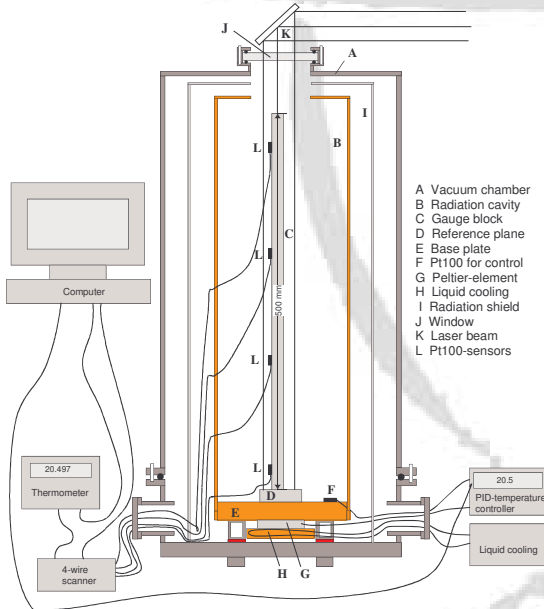
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## Abstract

- In precision length measurements the accurate and traceable value of the linear thermal expansion coefficient (LTEC) is needed
- A dilatometer that utilises a gauge block interferometer for relative length measurement has been constructed
- Standard uncertainty of  $0,02 \times 10^{-6} \text{ 1/K}$  for LTEC of gauge block has been reached

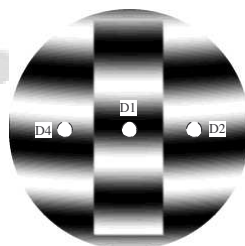
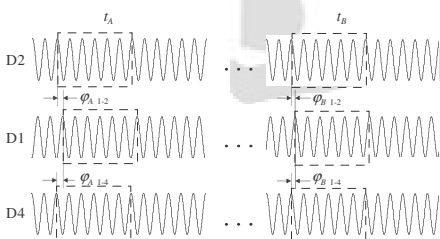
## Instrument composition

- The main solution is to measure the lengthening of a sample by interferometry in a vacuum
- A vacuum environment was selected due to its easiness with a refractive index of medium ( $n$ ) determination
- The problem with a vacuum solution is that thermal stabilisation times are longer due to the absence of convection



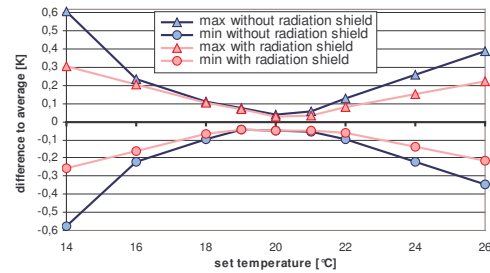
- The measurement of phase difference between the gauge block surface and the reference platen is repeated at proper intervals in order to follow number of full periods
- The simulated interferogram of static state of the gauge block interferometer and phase difference measurement principle are illustrated below.

$$\Delta L = \left( \frac{\varphi_{B1-2} + \varphi_{B1-4}}{2} - \frac{\varphi_{A1-2} + \varphi_{A1-4}}{2} \right) \frac{\lambda}{4\pi}$$

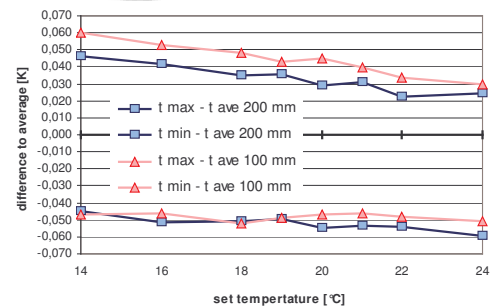


## Temperature control and measurements

- In order to allow fast operation and minimise temperature differences, the radiation cavity was constructed of copper
- A radiation shield is placed between the cavity and the chamber wall
- The temperature is set by changing the temperature of a base plate with two peltier elements (electric power 150 W)
- Temperature gradients inside the cavity were studied by connecting 4 Pt100 sensors at different heights and setting the controller from 14 to 24 °C



- The temperature of the sample is measured with four calibrated Pt100 sensors and a thermometer
- When the temperature differences of sensors no longer diminish, the relative expansion is measured and recorded together with the temperature values
- Typical temperature gradients in a 100 mm and 200 mm steel gauge blocks are illustrated here



## Uncertainty

The model of LTEC measurement for analysis of the uncertainty can be expressed as follows:

$$\alpha = \frac{1}{L} \frac{\Delta L + \delta l_p}{\Delta T + \delta t_g}$$

where  $\delta l_p$  is the correction to compensate for the non-linearity of the interferometer and  $\delta t_g$  is the correction due to the temperature differences of the gauge block

Quantity	Standard uncertainty	Probability distribution	Sensitivity coefficient	Standard uncertainty $\times 10^{-6} \text{ 1/K}$
$L$	2 $\mu\text{m}$	normal	$-5,5 \times 10^{-5} \text{ m}^{-1} \text{ K}^{-1}$	0,00011
$\Delta L$	0,001 $\mu\text{m}$	normal	$5 \text{ m}^{-1} \text{ K}^{-1}$	0,005
$\delta l_p$	0,001 $\mu\text{m}$	rectangular	$5 \text{ m}^{-1} \text{ K}^{-1}$	0,005
$\Delta T$	4 mK	normal	$-2,75 \times 10^{-6} \text{ K}^{-2}$	0,011
$\delta t_g$	5 mK	normal	$-2,75 \times 10^{-6} \text{ K}^{-2}$	0,014
Total	$L=100 \text{ mm}$			0,021

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